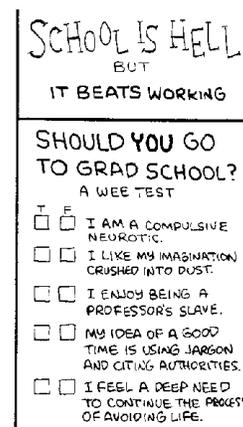
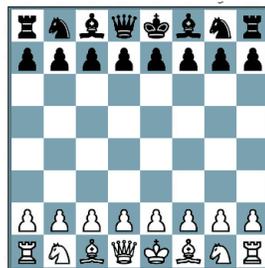


Classical Conditioning II: Learning from prediction errors



PSY/NEU338: Animal learning and decision making:
Psychological, computational and neural perspectives

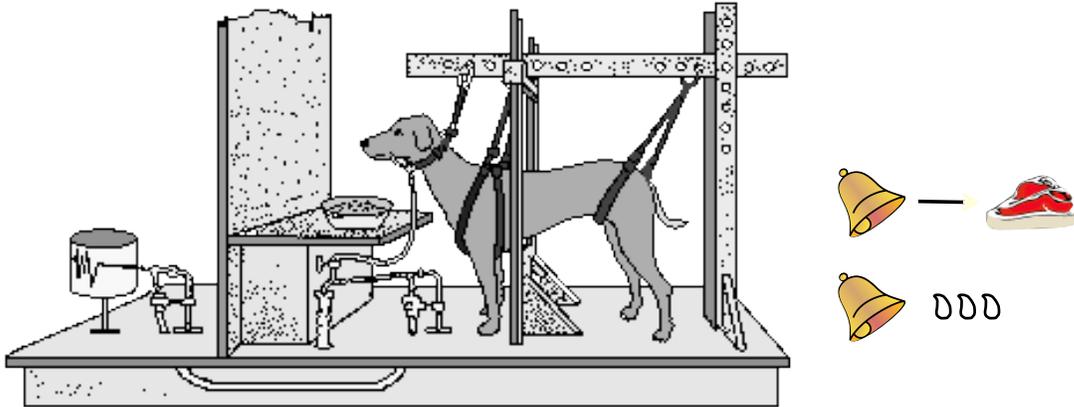
where were we?



decision making is hard

- Reward/punishment may be delayed
 - Outcomes may depend on a series of actions
- ⇒ “credit assignment problem” (Sutton, 1978)

predicting the future can help...
...and animals learn predictions!



3

examples of classical
conditioning from daily life

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outline

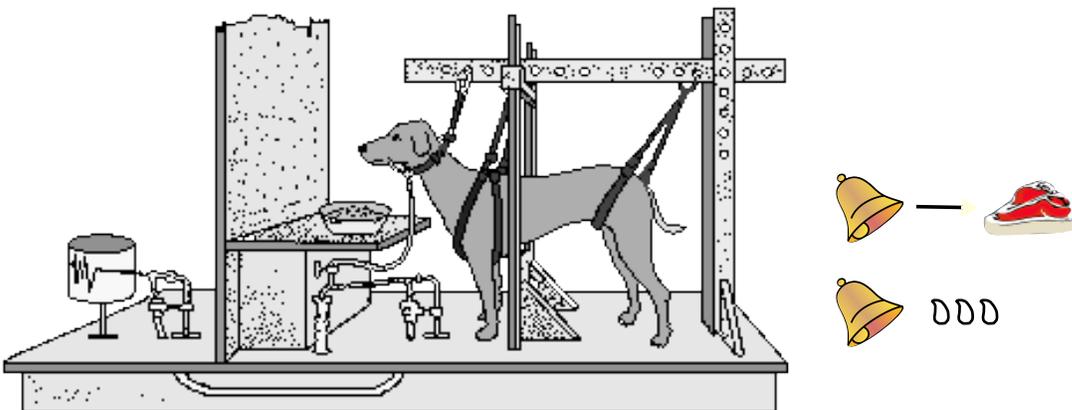
PART I - Basics of classical conditioning

PART II - Some challenging results

PART III - A theory (model)

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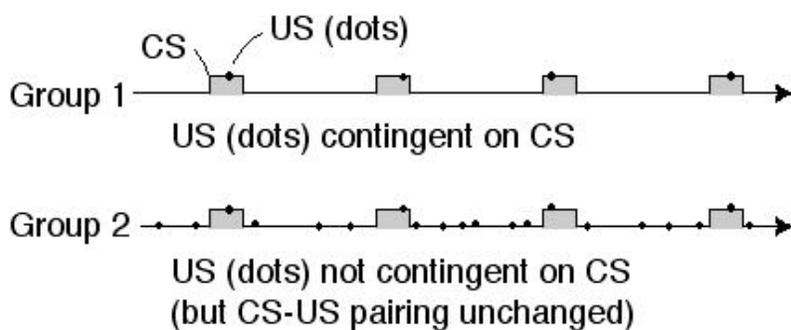
predicting the future can help...
...and animals learn predictions!



“pairing a tone (CS) and food (US) is sufficient to induce classical conditioning (prediction learning)”

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But... 1) Rescorla's control condition



will Group 2 show a CR to the tone?

temporal contiguity is not enough - need contingency

$$P(\text{food} \mid \text{tone}) > P(\text{food} \mid \text{no tone})$$

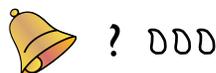
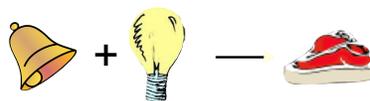
Credits: Randy Gallistel 7

But... 2) Kamin's blocking

Phase I



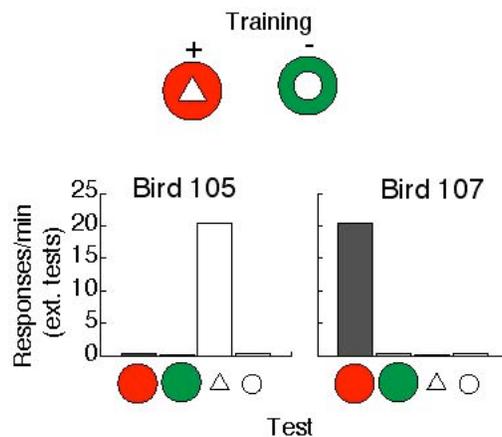
Phase II



contingency is also not enough.. need surprise

$$P(\text{food} \mid \text{noise+light}) \neq P(\text{food} \mid \text{noise alone})$$

And... 3) Reynold's overshadowing



stimuli compete for learning

Credits: Randy Gallistel 9

Summary so far...

- Naïvely it seemed that pairing a CS and a US is enough for conditioning (prediction learning)...
- But now we see that we also need contingency and surprise
- And that different stimuli compete for learning such that even with contingency and surprise learning is not guaranteed
- What is going on here?

outline

PART I - Basics of classical conditioning

PART II - Some challenging results

PART III - A theory (model)

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desiderata/goals of a learning theory

- Explain why the CS comes to elicit a response
- When (under what conditions) does this happen?
- Basic phenomena: gradual learning and extinction curves
- More elaborate behavioral phenomena (blocking, overshadowing)
- (explain neural data)

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Rescorla & Wagner (1972)



The idea: error-driven learning

Change in value is proportional to the difference between actual and predicted outcome

$$\Delta V(CS_i) = \eta [R_{US} - \sum_{j \in \text{trial}} V(CS_j)]$$

Two assumptions/hypotheses:

- (1) learning is driven by error (formalize notion of surprise)
- (2) summations of predictors is linear

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Rescorla & Wagner (1972)

Lets assume a simpler scenario: one CS and one US only

$$\Delta V = \eta [R - V]$$

$$\Delta V(CS_i) = \eta [R_{US} - \sum_{j \in \text{trial}} V(CS_j)]$$

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Rescorla & Wagner (1972)

Lets assume a simpler scenario: one CS and one US only

$$\Delta V = \eta[R - V]$$

or: $V_{T+1} = V_T + \eta[R_T - V_T]$ (note: T counts trials)

imagine a scenario with 50% reinforcement: 11010001101

1) what would V be on average after learning?

- a. $V = 1$
- b. $V = 0.5$
- c. $V = 0$
- d. it is impossible to know

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Rescorla & Wagner (1972)

Lets assume a simpler scenario: one CS and one US only

$$\Delta V = \eta[R - V]$$

or: $V_{T+1} = V_T + \eta[R_T - V_T]$ (note: T counts trials)

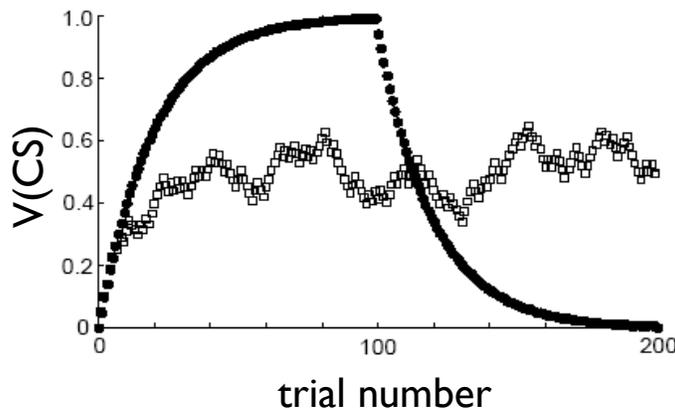
imagine a scenario with 50% reinforcement: 11010001101

2) what would the prediction error be after learning?

- a. PE = 1
- b. PE = 0.5
- c. PE = 0
- d. it depends on the trial

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Rescorla & Wagner (1972)



Can you estimate what learning rate (or step size) η was used in this simulation?
 (try to think how you could do the same from behavioral data)

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Rescorla & Wagner (1972)

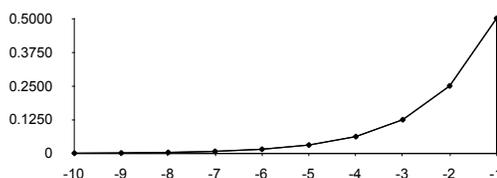
$$V_{T+1} = V_T + \eta[R_T - V_T]$$

how is the value (=prediction) in trial $(T+1)$ influenced by reinforcements on trials $(T), (T-1), (T-2) \dots$?

$$V_{T+1} = V_T(1 - \eta) + \eta R_T$$

$$V_{T+1} = \eta \sum_{i=0}^T (1 - \eta)^{T-i} R_i$$

the R-W rule predicts reinforcement using a weighted average of past reinforcements



Recent reinforcements are weighted more heavily.
 Why is this sensible?
 Learning rate = forgetting rate!

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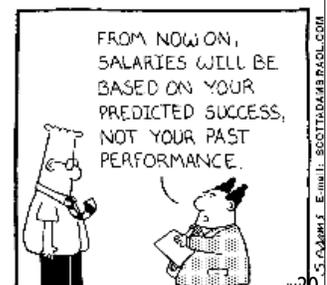
what does the theory explain?

| | R-W | |
|------------------------|-----|--|
| acquisition | ✓ | |
| extinction | ✗ | |
| blocking | ✓ | |
| overshadowing | ✓ | |
| temporal relationships | ✗ | |
| overexpectation | ✓ | |

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Summary so far...

- Animals learn predictions (classical conditioning can be seen as a “pure” instance of prediction learning)
- Prediction learning can be explained by an error-correcting learning rule: predictions are learned from experiencing the world and comparing predictions to reality (ie, learning from prediction errors)
- R-W: A simple model - but very powerful!



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optional reading

Rescorla & Wagner (1972) - *A theory of Pavlovian conditioning: Variations in the effectiveness of reinforcement and nonreinforcement* - the original chapter that is so well cited (and well written!)



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self-practice questions

1. What is an error-correcting learning rule?

2. How does the Rescorla-Wagner learning rule explain the phenomenon of blocking?

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